CHAPTER 6

Lines in 2 Dimensions

TOPIC 1: DISTANCE BETWEEN TWO POINTS AND SECTION FOR-MULA

VERY SHORT ANSWER TYPE QUESTIONS

Find the value of a, for which point $P(\frac{a}{3},2)$ is the 1. midpoint of the line segment joining the Points Q(-5,4) and R(-1,0).

[Board Sample Paper, 2016] Ans :

As per question, line diagram is shown below.

$$\begin{array}{ccc} Q & P & R \\ \bullet & & \\ (-5,4) & & \\ & \left(\frac{a}{3},2\right) & \\ \end{array}$$

Since P is mid-point of QR, we have

$$\frac{a}{3} = \frac{-5 + (-1)}{2} = \frac{-6}{2} = -3$$

or.

The ordinate of a point A on y-axis is 5 and B has 2. co-ordinates (-3, 1). Find the length of AB. Ans:

a = -9

[Delhi CBSE, Term-2, 2014]

We have A(0,5) and B(-3,1).

Distance between A and B,

$$AB = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

= $\sqrt{(-3 - 0)^2 + (1 - 5)^2}$
= $\sqrt{9 + 16}$
= $\sqrt{25} = 5$

Find the perpendicular distance of A(5, 12) from the 3. y-axis.

Ans : [Board Terms-2, 2011 Set (A1)]

As per question, line diagram is shown below. Perpendicular from point A(5,12) on y-axis touch it at (0, 12).

Distance between (5,12) and (0,12) is,

$$d = \sqrt{(0-5)^2 + (12-12)^2}$$

$$=\sqrt{25}$$

= 5 units.

If the centre and radius of circle is (3, 4) and 7 units 4. respectively,, then what it the position of the point A(5,8) with respect to circle?

[Board Term-2, 2013] Ans :

Distance of the point, from the centre

$$a = \sqrt{(5-3)^2 + (8-4)^2}$$
$$= \sqrt{4+16} = \sqrt{20} = 2\sqrt{5}$$

Since $2\sqrt{5}$ is less than 7, the point lies inside the circle.

Find the perimeter of a triangle with vertices 5. (0,4),(0,0) and (3,0).

[Board Term-2, 2011 Set (B1)]

We have A(0,4), B(0,0), and C(3,0). $AB = \sqrt{(0-2)^2 + (0-4)^2} = \sqrt{16} = 4$

$$BC = \sqrt{(3-0)^2 + (0-0)^2} = \sqrt{9} = 3$$

$$CA = \sqrt{(0-3)^2 + (4-0)^2}$$

$$= \sqrt{9+16} = \sqrt{25} = 5$$

Thus Perimeter of triangle = 4 + 3 + 5 = 12

To locate a point Q on line segment AB such that $BQ = \frac{5}{7} \times AB$. What is the ratio of line segment in which AB is divided? Ans :

 $BQ = \frac{5}{7}AB$

[Board Term-2, 2013]

We have

Ans :

Ans :

$$\frac{BQ}{AB} = \frac{5}{7} \Rightarrow \frac{AB}{BQ} = \frac{7}{5}$$
$$\frac{AB - BQ}{BQ} = \frac{AQ}{BQ} = \frac{7 - 5}{5} = \frac{2}{5}$$
$$AQ:BQ = 2:5$$

7. Find the distance of the point (-4, -7) from the y-axis.

As per question, line diagram is shown below. Perpendicular from point A(-4, -7) on y-axis touch it at (0, -7).

Distance between
$$(-4, -7)$$
 and $(0, -7)$ is
 $d = \sqrt{(0+4)^2 + (-7+7)^2}$
 $= \sqrt{4^2 + 0} = \sqrt{16} = 4$ units

8. If the distance between the points (4, k) and (1, 0) is 5, then what can be the possible values of k. Ans :

[Delhi Set I, II, III 2017]

Using distance formula

V

$$\sqrt{(4-1)^2 + (k-0)^2} = 5$$

3² + k² = 25
k ± 4

Find the coordinates of the point on y-axis which is 9. nearest to the point (-2,5). Ans :

[Sample Question Poper, 2017]

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The point on y-axis that is nearest to the point (-2,5) is (0,5).

10. In what ratio does the x-axis divide the line segment joining the points (-4, -6) and (-1, 7)? Find the coordinates of the point of division.

Ans :

[Board Sample Paper, 2017]

Let x-axis be divides the line-segment joining (-4, -6) and (-1, 7) at the point P(x, y) in the ratio 1:k.

Now, the coordinates of point of division P,

$$(x,y) = \frac{1(-1) + k(-4)}{k+1}, \frac{1(7) + k(-6)}{k+1}$$
$$= \frac{-1 - 4k}{k+1}, \frac{7 - 6k}{k+1}$$

Since P lies on x axis, therefore y = 0, which gives

$$\frac{7-6k}{k+1} = 0$$
$$7-6k = 0$$
$$k = \frac{7}{6}$$

Hence, the ratio is $1:\frac{7}{6}$ or, 6:7 and the coordinates of P are $\left(-\frac{34}{13}, 0\right)$

SHORT ANSWER TYPE QUESTIONS - I

Find a relation between x and y such that the point 1. P(x,y) is equidistant from the points A(-5,3) and B(7,2).

[Board Sample Paper, 2016]

Let P(x,y) is equidistant from A(-5,3) and B(7,2), then we have

$$AP = BP$$

$$\sqrt{(x+5)^2 + (y-3)^2} = \sqrt{(x-7)^2 + (y-2)^2}$$

$$(x+5)^2 + (y-3)^2 = (x-7)^2 + (y-2)^2$$

$$10x + 25 - 6y + 9 = -14x + 49 - 4y + 4$$

$$24x + 34 = 2y + 53$$

$$24x - 2y = 19$$

Thus 24x - 2y - 19 = 0 is the required relation.

The x-coordinate of a point P is twice its y-coordinate. 2. If P is equidistant from Q(2, -5) and R(-3, 6), find the co-ordinates of P.

Ans :

Let the point P(2y, y),

Since
$$PQ = PR$$
, we have
 $\sqrt{(2y-2)^2 + (y+5)^2} = \sqrt{(2y+3)^2 + (y-6)^2}$
 $(2y-2)^2 + (y+5)^2 = (2y+3)^2 + (y-6)^2$
 $-8y+4+10y+25 = 12y+9-12y+36$
 $2y+29 = 45$
 $y = 8$

Hence, coordinates of point P are (16,8)

Find the ratio in which y-axis divides the line segment 3. joining the points A(5, -6) and B(-1, -4). Also find

the co-ordinates of the point of division.

[Delhi Set I, II, III, 2016]

Let y-axis be divides the line-segment joining A(5,-6) and B(-1,-4) at the point P(x,y) in the ratio AP: PB = k:1

Now, the coordinates of point of division P,

$$(x,y) = \frac{k(-1)+1(5)}{k+1}, \quad \frac{k(-4)+1(-6)}{k+1}$$
$$= \frac{-k+5}{k+1}, \quad \frac{-4k-6}{k+1}$$

Since P lies on y axis, therefore x = 0, which gives

$$\frac{5-k}{k+1} = 0$$

k = 5

Hence required ratio is 5:1

Now

Ans:

 $y = \frac{-4(5)-6}{6} = \frac{-13}{3}$

Hence point on y-axis is $(0, -\frac{13}{3})$.

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Ans :

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- For School Education
- Find the ratio in which the point (-3, k) divides the 4. line segment joining the points (-5, -4) and (-2, 3). Also find the value of k.

[Foreign Set I, II, III, 2016]

As per question, line diagram is shown below.

Let AB be divides by P in ratio n:1. x co-ordinate for section formula

> $-3 = \frac{(-2)n + 1(-5)}{n+1}$ -3(n+1) = -2n-5-3n-3 = -2n-55 - 3 = 3n - 2n2 = n $\frac{n}{1} = \frac{2}{1}$ or 2:1

Ratio Now, y co-ordinate.

 $k = \frac{2(3) + 1(-4)}{2+1} = \frac{6-4}{3} = \frac{2}{3}$

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[Delhi Set I, II, III, 2016]

5. If the point P(x,y) is equidistant from the points Q(a+b,b-a) and R(a-b,a+b), then prove that bx = ay.

Ans :

We have
$$|PQ| = |PR|$$

 $\sqrt{[x-(a+b)]^2 + [y-(b-a)]^2}$
 $= \sqrt{[x-(a-b)]^2 + [y-(b+a)]^2}$



$$\begin{aligned} \left[x - (a+b)\right]^2 + \left[y - (b-a)\right]^2 \\ &= \left[x - (a-b)\right]^2 + \left[y - (a+b)\right]^2 \\ -2x(a+b) - 2y(b-a) &= -2x(a-b) - 2y(a+b) \\ 2x(a+b) + 2y(b-a) &= 2x(a-b) + 2y(a+b) \\ 2x(a+b-a+b) + 2y(b-a-a-b) &= 0 \\ 2x(2b) + 2y(-2a) &= 0 \\ xb - ay &= 0 \\ bx &= ay \end{aligned}$$
Hence Proved

6. Prove that the point (3,0), (6,4) and (-1,3) are the vertices of a right angled isosceles triange.

Ans :

We have A(3,0), B(6,4) and C(-1,3)Now $AB^2 = (3-6)^2 + (0-4)$

$$AB^{2} = (3-6)^{2} + (0-4)^{2}$$

= 9 + 16 = 25
$$BC^{2} = (6+1)^{2} + (4-3)^{2}$$

= 49 + 1 = 50
$$CA^{2} = (-1-3)^{2} + (3-0)^{2}$$

= 16 + 9 = 25
$$AB^{2} = CA^{2} \text{ or, } AB = CA$$

[O.D. Set I, II, III, 2016]

Hence triangle is isosceles.



Also,
$$25 + 25 = 50$$

or, $AB^2 + CA^2 = BC^2$

Since pythagoras theorem is verified, therefore triangle is a right angled triangle.

7. If A(5,2), B(2,-2) and C(-2,t) are the vertices of a right angled triangle with $\angle B = 90^{\circ}$, then find the value of t.

Ans : [Delhi CBSE Board, 2015][Set I, II, III]

As per question, triangle is shown below.



Now
$$AB^2 = (2-5)^2 + (-2-2)^2 = 9 + 16 = 25$$

 $BC^2 = (-2-2)^2 + (t+2)^2 = 16 + (t+2)^2$
 $AC^2 = (5+2)^2 + (2-t)^2 = 49 + (2+t^2)$
Since $\triangle ABC$ is a right angled triangle
 $AC^2 = AB^2 + BC^2$
 $49 + (2-t)^2 = 25 + 16 + (t+2)^2$
 $49 + 4 - 4t + t^2 - 41 + t^2 + 4t + 4$

$$53 - 4t = 45 + 4t$$
$$8t = 8$$
$$t = 1$$

8. Find the ratio in which the pont P(³/₄, ⁵/₁₂) divides the line segment joining the point A (¹/₂, ³/₂) and (2, -5). Ans: [Delhi CBSE Term-2, 2015, Set I, II, III] Let P divides AB in the ration k:1. Line diagram is

Let P divides AB in the ratio k: 1. Line diagram is shown below.

$$A \xrightarrow{P\left(\frac{3}{4},\frac{5}{12}\right)} B \xrightarrow{k:1} (2,-5)$$

Now $\frac{k(2) + 1(\frac{1}{2})}{k+1} = \frac{3}{4}$ 8k+2 = 3k+3 $k = \frac{1}{5}$

Thus required ratio is $\frac{1}{5}$:1 or 1:5.

9. The points (4,7), B(p,3) and C(7,3) are the vertices of a right triangle, right-angled at B. Find the value

of *p*.

Ans : [Outside Delhi CBSE, 2015, Set I, II]

As per question, triangle is shown below. Here ΔABC is a right angle triangle,



$$AB^{2} + BC^{2} = AC^{2}$$

$$(p-4)^{2} + (3-7)^{2} + (7-p)^{2} + (3-3)^{2}$$

$$= (7-4)^{2} + (3-4)^{2}$$

$$(p-4)^{2} + (-4)^{2} + (7-p)^{2} + 0 = (3)^{2} + (-4)^{2}$$

$$p^{2} - 8p + 16 + 16 + 49 + p^{2} - 14p = 9 + 16$$

$$2p^{2} - 22p + 81 = 25$$

$$2p^{2} - 22p + 81 = 25$$

$$2p^{2} - 22p + 56 = 0$$

$$p^{2} - 11p + 28 = 0$$

$$(p-4)(p-7) = 0$$

$$p = 7 \text{ or } 4$$

10. If A(4,3), B(-1,y), and C(3,4) are the vertices of a right triangle ABC, right angled at A, then find the value of y.

Ans : [Outside Delhi Board, 2015, Set II]

As per question, triangle is shown below.



We have

$$(4+1)^{2} + (3-y)^{2} + (4-3)^{2} = (3+1)^{2} + (4-y)^{2}$$

$$(5)^{2} + (3-y)^{2} + (-1)^{2} + (1)^{2} = (4)^{2} + (4-y)^{2}$$

$$25+9-6y+y^{2}+1+1 = 16+16-8y+y^{2}$$

$$36+2y-32 = 0$$

$$2y+4 = 0$$

$$y = -2$$

 $AB^2 + AC^2 = BC^2$

11. Show that the points (a, a), (-a, -a) and Get all GUIDE and Sample Paper PDFs by whatsapp from +91 89056 29969 www.rava.org.in

 $\left(-\sqrt{3} a, \sqrt{3} a\right)$ are the vertices of an equilateral triangle.

Ans: [Foreign Set I, II, III, 2015]

Let
$$A(a, a), B(-a, -a)$$
 and $C(-\sqrt{3} a, \sqrt{3} a)$
 $AB = \sqrt{(a+a)^2 + (a+a)^2}$
 $= \sqrt{4a^2 + 4a^2}$
 $= 2\sqrt{2} a$
 $BC = \sqrt{(-a+\sqrt{3} a)^2 + (-a-\sqrt{3} a)^2}$
 $= \sqrt{a^2 - 2\sqrt{3} a^2 + 3a^2 + a^2 + 2\sqrt{3} a^2 + 3a^2}$
 $= 2\sqrt{2} a$
 $AC = \sqrt{(a+\sqrt{3} a)^2 + (a-\sqrt{3} a)^2}$

 $= \sqrt{a^2 + 2\sqrt{3} a^2 + 3a^2 + a^2 - 2\sqrt{3} a^2 + 3a^2}$ = $2\sqrt{2} a$ Since AB = BC = AC, therefore ABC is an equilateral triangle.

12. If the mid-point of the line segment joining $A\left[\frac{x}{2}, \frac{y+1}{2}\right]$ and B(x+1, y-3) is C(5, -2), find x, y. Ans: [Delhi CBSE, Term II, 2014][Board Term-2, 2012 Set (1)] If the mid-point of the line segment joining $A\left[\frac{x}{2}, \frac{y+1}{2}\right]$ and B(x+1, y-3) is C(5, -2), then at mid point,

$$\frac{\frac{x}{2} + x + 1}{2} = 5$$
$$\frac{3x}{2} + 1 = 10$$
$$3x = 18$$
$$x = 6$$
$$\frac{\frac{y+1}{2} + y - 3}{2} = -2$$

or,

also

Ans :

$$\frac{y}{2} + y - 3 = -4$$

y+1+2y-6 = -8
y = -1

y + 1 .

13. Find the point on the x-axis which is equidistant from the points (2, -5) and (-2, 9).

Let the point P(x, 0) on the x-axis is equidistant from points A(2, -5) and B(-2, 9).

$$PA^{2} = PB^{2}$$

$$(2 - x)^{2} + (-5 - 0)^{2} = (-2 - x)^{2} + (9 - 0)^{2}$$

$$4 - 4x + x^{2} + 25 = 4 + 4x + x^{2} + 81$$

$$-8x = 56$$

$$x = -7$$

Thus point is (-7, 0).

14. Show that A(6,4), B(5,-2) and C(7,-2) are the vertices of an isosceles triangle.
Ans: [Board Term-2, 2012 Set (44)] We have A(6,4), B(5,-2), C(7,-2).

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Now
$$AB = \sqrt{(6-5)^2 + (4+2)^2}$$

 $= \sqrt{1^2 + 6^2} = \sqrt{37}$
 $BC = \sqrt{(5-7)^2 + (-2+2)^2}$
 $= \sqrt{(-2)^2 + 0^2} = 2$
 $CA = \sqrt{(7-6)^2 + (-2-4)^2}$
 $= \sqrt{1^2 + 6^2} = \sqrt{37}$
 $AB = BC = \sqrt{37}$

Since two sides of a triangle are equal in length, triangle is an isosceles triangle.

15. If P(2, -1), Q(3, 4), R(-2, 3) and S(-3, -2) be four points in a plane, show that PQRS is a rhombus but not a square.

Ans :

We have
$$P(2, -1), Q(3, 4), R(-2, 3), S(-3, -2)$$

 $PQ = \sqrt{1^2 + 5^2} = \sqrt{26}$
 $QR = \sqrt{5^2 + 1^2} \sqrt{26}$
 $RS = \sqrt{1^2 + 5^2} = \sqrt{26}$
 $PS = \sqrt{5^2 + 1^2} = \sqrt{26}$

Since all the four sides are equal, PQRS is a rhombus.



Now
$$PR = \sqrt{1^2 + 5^2} = \sqrt{26}$$

 $= \sqrt{4^2 + 4^2} = \sqrt{32}$

 $PQ^{2} + QR^{2} = 2 \times 26 = 52 \neq (\sqrt{32})^{2}$ Since ΔPQR is not a right triangle, PQRS is a rhombus but not a square.

Show that A(-1,0), B(3,1), C(2,2) and D(-2,1) are 16. the vertices of a parallelogram ABCD.

[Board Term-2, 2012 Set (1)]

[Board Term-2, 2012 (28)]

Mid-point of AC

Ans :

$$\left(\frac{-1+2}{2}, \frac{0+2}{2}\right) = \left(\frac{1}{2}, 1\right)$$

Mid-point BD

$$\left(\frac{3-2}{2}, \frac{1+1}{2}\right) = \left(\frac{1}{2}, 1\right)$$

Here Mid-point of AC = Mid-point of BDSince diagonals of a quadrilateral bisect each other, ABCD is a parallelogram.

17. If (3,2) and (-3,2) are two vertices of an equilateral triangle which contains the origin, find the third vertex.

[Board Term-2, 2012 Set (12)] Ans : We have A(3,2) and B(-3,2).

It can be easily seen that mid-point of AB is lying on y-axis. Thus AB is equal distance from x-axis everywhere.

Also $OD \perp AB$

Hence 3^{rd} vertex of ΔABC is also lying on y-axis. The digram of triangle should be as given below.



Let C(x, y) be the coordinate of 3^{rd} vertex of ΔABC .

Now
$$AB^2 = (3+3)^2 + (2-BC^2) = (x+3)^2 + (y-AC^2) = (x-3)^2 + (y-AC^2) = (x-3)^2 + (y-AC^2) = AC^2 = BC^2$$

Since $AB^2 = AC^2 = BC^2$

 $(m+2)^2 + (m+2)^2$

$$(x+3)^{2} + (y-2)^{2} = 36$$
(1)

$$(x-3)^{2} + (y-2)^{2} = 36$$
(2)

 $(x-3)^2 + (y-2)^2 = 36$ Since P(x, y) lie on y-axis, substituting x = 0 in(1) we have

$$3^{2} + (y - 2)^{2} = 36 - 9 = 27$$

 $(y - 2)^{2} = 36 - 9 = 27$

Taking square root both side

$$y-2 = \pm 3\sqrt{3}$$
$$y = 2 \pm 3\sqrt{3}$$

Since origin is inside the given triangle, coordinate of C below the origin,

$$y = 2 - 3\sqrt{3}$$

Hence Coordinate of C is $(0, 2 - 3\sqrt{3})$

18. Find a so that (3, a) lies on the line represented by 2x - 3y - 5 = 0. Also, find the co-ordinates of the point where the line cuts the x-axis.

 $(2)^2 = 36$

 $(2)^2$ $2)^{2}$

Since (3, a) lies on 2x - 3y - 5 = 0, it must satisfy this equation. Therefore

$$2 \times 3 - 3a - 5 = 0$$

$$6 - 3a - 5 = 0$$

$$1 = 3a$$

$$a = \frac{1}{3}$$

Line 2x - 3y - 5 = 0 will cut the x-axis at (x, 0). and it must satisfy the equation of line.

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Ans :

$$2x - 5 = 0 \implies x = \frac{5}{2}$$

Hence point is $\left(\frac{5}{2}, 0\right)$

19. If the vertices of $\triangle ABC$ are A(5, -1), B(-3, -2),C(-1,8), Find the length of median through A. Ans : [Board Term-2, 2012 Set (17)]

Let AD be the median. As per question, triangle is shown below.



Since D is mid-point of BC, co-ordinates of D,

$$x_{1}, y_{2}) = \left(\frac{-3-1}{2}, \frac{-2+8}{2}\right)$$
$$= (-2, 3)$$
$$AD = \sqrt{(5+2)^{2} + (-1-3)^{2}}$$
$$= \sqrt{(7)^{2} + (4)^{2}}$$
$$= \sqrt{49 + 16}$$
$$= \sqrt{65} \text{ units}$$

Thus length of median is $\sqrt{65}$

(

20. Find the mid-point of side BC of ΔABC , with A(1, -4) and the mid-points of the sides through A being (2, -1) and (0, -1).

[Board Term-2, 2012 Set (21)]

Assume co-ordinates of B and C are (x_1, y_1) and (x_2, y_2) respectively. As per question, triangle is shown below.



Now



$$0 = \frac{1+x_2}{2} \Rightarrow x = -1$$
$$-1 = \frac{-4+y_2}{2} \Rightarrow y_2 = -1$$

 $2 = \frac{1+x_1}{2} \Rightarrow x_1 = 3$

 $-1 = \frac{-4 + y_1}{2} \Rightarrow y_1 = 2$

Thus
$$B(x_1, y_1) = (3, 2),$$

 $C(x_2, y_2) = (-1, 2)$
So, mid-point of *BC* is $\left(\frac{3-1}{2}, \frac{2+2}{2}\right) = (1, 2)$

21. A line intersects the y-axis and x-axis at the points Pand Q respectively. If (2, -5) is the mid-point of PQ, then find the coordinates of P and Q.

[Outside Delhi, Set-III, 2017]

Let coordinates of P be (0, y) and of Q be (x, 0). A(2, -5) is mid point of PQ.

As per question, line diagram is shown below.



Using section formula,

and

Thus

Ans :

$$(2, -5) = \left(\frac{0+x}{2} + \frac{y+0}{2}\right)$$
$$2 = \frac{x}{2} \Rightarrow x = 4$$
$$-5 = \frac{y}{2} \Rightarrow y = -10$$
$$P \text{ is } (0, -10) \text{ and } Q \text{ is } (4, 0)$$

22. If $(1, \frac{p}{3})$ is the mid point of the line segment joining the points (2,0) and $(0,\frac{2}{9})$, then show that the line 5x + 3y + 2 = 0 passes through the point (-1, 3p). Ans :

Since $(1, \frac{p}{3})$ is the mid point of the line segment joining the points (2,0) and $(0,\frac{2}{9})$, we have

$$\frac{p}{3} = \frac{0 + \frac{2}{9}}{2} = \frac{1}{9}$$
$$p = \frac{1}{3}$$

Now the point (-1, 3p) is (-1, 1). The line 5x + 3y + 2 = 0, passes through the point (-1,1) as 5(-5) + 3(1) + 2 = 0

23. If two adjacent vertices of a parallelogram are (3,2)and (-1,0) and the diagonals intersect at (2,-5)then find the co-ordinates of the other two vertices. Ans : [Board Foreign Set I, II, III, 2017]

Let two other co-ordinates be (x, y) and (x, y')respectively using mid-point formula.

As per question parallelogram is shown below.

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 $2 = \frac{x+3}{2} \Rightarrow x = 1$

 $-5 = \frac{2+y}{2} \Rightarrow y = -12$

Now

and

Again, $\frac{-1+x'}{2} = 2 \Rightarrow x' = 5$

and $\frac{0+y'}{2} = -5 \Rightarrow y' = -10$ Hence, coordinates of C(1, -12) and D(5, -10)

24. In what ratio does the point P(-4,6) divides the line segment joining the points A(-6,10) and B(3,-8)?
Ans: [Delhi Compt. Set-I, II, III 2017]

Let Now

 $\frac{3k-6}{k+1} = -4$ 3k-6 = -4k-47k = 2 $k = \frac{7}{2}$

AP:PB = k:1

]

Hence, AP:PB = 7:2

25. If the line segment joining the points A(2,1) and B(5,-8) is trisected at the points P and Q, find the coordinates P.

Ans :

[Outside Delhi Compt. Set-I, III, 2017]

As per question, line diagram is shown below.

Let P(x,y) divides AB in the ratio 1:2 Using section formula we get

$$x = \frac{1 \times 5 + 2 \times 2}{1 + 2} = 3$$
$$y = \frac{1 \times -8 + 2 \times 1}{1 + 2} = 2$$

Hence coordinates of P are (3, -2).

SHORT ANSWER TYPE QUESTIONS - II

1. If the point C(-1,2) divides internally the line segment joining the points A(2,5) and B(x,y) in the

ratio 3:4, find the value of $x^2 + y^2$. **Ans :** [Foreign Set I, II, III, 2016]

As per question, line diagram is shown below.

$$\begin{array}{c} 3:4\\ A & C & B\\ \bullet & & \\ (2,5) & (-1,2) & (x,y) \end{array}$$

We have $\frac{AC}{BC} = \frac{3}{4}$

Applying section formula for x co-ordinate,

$$-1 = \frac{3x + 4(2)}{3 + 4}$$
$$-7 = 3x + 8$$
$$x = -5$$

Similarly applying section formula for y co-ordinate, 3y + 4(5)

$$2 = \frac{3y+4(3)}{3+4}$$
$$14 = 3y+20$$
$$y = 2$$

Thus (x, y) is (-5, -2). Now $x^2 + y^2 = (-5)^2 + (-2)^2$ = 25 + 4 = 29

2. If the co-ordinates of points A and B are (-2, -2) and (2, -4) respectively, find the co-ordinates of P such that AP = ³/₇AB, where P lies on the line segment AB.
Ans: [Outside Delhi, 2015, Set I, II]

We have $AP = \frac{3}{7}AB \Rightarrow AP:PB = 3:4$

As per question, line diagram is shown below.

Section formula :

$$x = \frac{mx_2 + nx_1}{m+n}$$
 and $y = \frac{my_2 + nx_1}{m+n}$

Applying section formula we get

$$x = \frac{3 \times 2 + 4 \times -2}{3 + 4} = -\frac{2}{7}$$
$$y = \frac{3 \times -4 + 4 \times -2}{3 + 4} = -\frac{20}{7}$$

Hence P is $\left(-\frac{2}{7}, -\frac{20}{7}\right)$

3. Find the co-ordinate of a point *P* on the line segment joining A(1,2) and B(6,7) such that $AP = \frac{2}{5}AB$ Ans : [Outside Delhi, 2015, Set III]

As per question, line diagram is shown below.

$$\begin{array}{c|cccc} A & P(x,y) & B \\ \hline \bullet & & \\ (1,2) & 2:3 & (6,7) \end{array}$$

We have

Section formula :

$$x = \frac{mx_2 + nx_1}{m+n}$$
 and $y = \frac{my_2 + nx_1}{m+n}$

 $AP = \frac{2}{5}AB \Rightarrow AP: PB = 2:3$

Applying section formula we get

$$x = \frac{2 \times 6 + 3 \times 1}{2 + 3} = \frac{12 + 3}{5} = 3$$

 $y = \frac{2 \times 7 + 3 \times 2}{2 + 3} = \frac{14 + 6}{5} = 4$

and

Thus P(x,y) = (3,4)

4. If the distance of P(x, y) from A(6, 2) and B(-2, 6) are equal, prove that y = 2x.

Ans: [CBSE Board Term-2, 2015]
We have
$$P(x,y), A(6,2), B(-2,6)$$

Now $PA = PB$
 $PA^2 = PB^2$
 $(x-6)^2 + (y-2)^2 = (x+2)^2 + (y-6)^2$
 $-12x+36-4y+4 = 4x+4-12y+36$
 $-12x-4y = 4x-12y$
 $12y-4y = 4x+12x$
 $8y = 16x$
 $y = 2x$ Hence Proved

5. The co-ordinates of the vertices of $\triangle ABC$ are A(7,2), B(9,10) and C(1,4). If E and F are the mid-points of AB and AC respectively, prove that $EF = \frac{1}{2}BC$. Ans: [Board Term-2 2015]

Let the mid-points of AB and AC be $E(x_1, y_1)$ and $F(x_2, y_2)$. As per question, triangle is shown below.



Co-ordinates of point E

$$(x_1, y_1) = \left(\frac{9+7}{2}, \frac{10+2}{2}\right) = (8, 6)$$

Co-ordinates of point ${\cal F}$

$$(x_2, y_2) = \left(\frac{7+1}{2}, \frac{2+4}{2}\right) = (4,3)$$

Length,

$$EF = \sqrt{(x-4)^2 + (6-3)^2}$$

= $\sqrt{(4)^2 + (3)^2}$

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$$= 5 \text{ units} \qquad \dots(1)$$

Length
$$BC = \sqrt{(9-1)^2 + (10-4)^2}$$
$$= \sqrt{(8)^2 + (6)^2}$$
$$= 10 \text{ units} \qquad \dots(2)$$

From equation (1) and (2) we get

E

$$F = \frac{1}{2}BC$$
 Hence proved.

6. Prove that the diagonals of a rectangle ABCD, with vertices A(2, -1), B(5, -1), C(5,6) and D(2,6) are equal and bisect each other.
Ans : [CBSE 0.D. 2014]

As per question, rectangle ABCD, is shown below.



Now
$$AC = \sqrt{(5-2)^2 + (6+1)^2} = \sqrt{3^2 + 7^2}$$

 $= \sqrt{9+49} = \sqrt{58}$
 $BD = \sqrt{(5-2)^2 + (-1-6)^2} = \sqrt{3^2 + 7^2}$
 $= \sqrt{9+49} = \sqrt{58}$

Since $AC = BD = \sqrt{58}$ the diagonals of rectangle ABCD are equal

Mid-point of AC

$$=\left(\frac{2+5}{2},\frac{-1+6}{2}\right)=\left(\frac{7}{2},\frac{5}{2}\right)$$

Mid-point of BD

Ans :

$$=\left(\frac{2+5}{2},\frac{6+-1}{2}\right)=\left(\frac{7}{2},\frac{5}{2}\right)$$

Since the mid-point of diagonal AC and mid-point of diagonal BD is same and equal to $\left(\frac{7}{5}, \frac{5}{2}\right)$. Hence they bisect each other.

7. Find the ratio in which the line segment joining the points A(3, -3) and B(-2, 7) is divided by x-axis. Also find the co-ordinates of point of division.

[Delhi, Term-2, 2014]

y co-ordinate of any point on the x will be zero. Let (x, 0) be point on x axis which cut the line. As per question, line diagram is shown below.

$$A \xleftarrow{k} P 1 \xrightarrow{B} B$$

$$(3,-3) (x,0) (2,-4)$$

Let the ratio be k:1.

Using section formula for y co-ordinate we have

$$0 = \frac{1(-3) + k(7)}{1+k}$$
$$k = \frac{3}{\pi}$$

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Using section formula for x co-ordinate we have

$$x = \frac{1(3) + k(-2)}{1+k} = \frac{3-2 \times \frac{3}{7}}{1+\frac{3}{7}} = \frac{3}{2}$$

Thus co-ordinates of point are $\left(\frac{3}{2}, 0\right)$.

8. Find the ratio in which (11,15) divides the line segment joining the points (15,5) and (9,20)
Ans: [board Term-2, 2014]

Let the two points (15,5) and (9,20) are divided in the ratio k:1 by point P(11,15)Using Section formula, we get

$$x = \frac{m_2 x_1 + m_1 x_2}{m_2 + m_1}$$
$$11 = \frac{1(15) + k(9)}{1 + k}$$
$$11 + 11k = 15 + 9k$$
$$k = 2$$

Thus ratio is 2:1.

9. Find the point on y-axis which is equidistant from the points (5, -2) and (-3, 2).
Ans: [Delhi Set, 2014]

[Delhi Set, 2014] [Board Term-2, 2012 Set (13)]

Let point be (0, y)

$$5^{2} + (y+2)^{2} = (3)^{2} + (y-2)^{2}$$

or, $y^{2} + 25 + 4y + 4 = 9 - 4y + 4$
 $8y = -16$ or, $y = -2$
or, Point $(0, -2)$

10. The vertices of $\triangle ABC$ are A(6, -2), B(0, -6) and C(4,8). Find the co-ordinates of mid-points of AB, BC and AC.

Let mid-point of AB, BC and AC be $D(x_1, y_1)$, $E(x_2, y_2)$ and $F(x_2, y_3)$. As per question, triangle is shown below.



Using section formula, the co-ordinates of the points D, E, F are

For D,

$$x_1 = \frac{6+0}{2} = 3$$
$$y_1 = \frac{-2-6}{2} = -4$$

For E,

 $x_2 = \frac{0+4}{2} = 2$

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For F,

$$y_3 = \frac{-2+8}{2} = 3$$

 $y_2 = \frac{-6+8}{2} = 1$

 $x_3 = \frac{4+6}{2} = 5$

The co-ordinates of the mid-points of AB, BC and AC are D(3, -4), E(2, 1) and F(5, 3) respectively.

11. Find the ratio in which the point (-3, p) divides the line segment joining the points (-5, -4) and (-2,3). Hence find the value of p.
Ans: [Board Term-2, 2012]

As per question, line diagram is shown below.

$$(-3, p)$$

$$(-5, -4) \qquad p \qquad (-2, 3)$$

Let X(-3,p) divides the line joining of A(-5,-4)and B(-2,3) in the ratio k:1. The co-ordinates of p are $\left[\frac{-2k-5}{k+1},\frac{3k-4}{k+1}\right]$ But co-ordinates of P are (-3,p). Therefore we get

$$\frac{-2k-5}{k+1} = -3 \Rightarrow k=2$$

and

Ans :

Substituting k = 2 gives

$$p = \frac{2}{3}$$

Hence ratio of division is 2:1 and $p = \frac{2}{3}$

 $\frac{3k-4}{k+1} = p$

12. Find the ratio in which the point p(m, 6) divides the line segment joining the points A(-4, 3) and B(2, 8). Also find the value of m.

[Board Term-2, 2012 set (31)]

As per question, line diagram is shown below.

Let the ratio be $k\!:\!1$

Using section formula, we have

$$m = \frac{2k + (-4)}{k+1} \tag{1}$$

$$6 = \frac{8k+3}{k+1}$$
(2)

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$$8k+3 = 6k+6$$
$$2k = 3$$
$$k = \frac{3}{2}$$

Thus ratio is $\frac{3}{2}$:1 or 3:2. Substituting value of k in (1) we have

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$$m = \frac{2\left(\frac{3}{2}\right) + \left(-4\right)}{\frac{3}{2} + 1} = \frac{3-4}{\frac{5}{2}} = \frac{-1}{\frac{5}{2}} = \frac{-2}{5}$$

13. If A(4, -1), B(5,3), C(2, y) and D(1,1) are the vertices of a parallelogram ABCD, find y.

[board Term-2, 2012 Set (5)]

Diagonals of a parallelogram bisect each other. Mid-points of AC and BD are same.

Thus
$$\left(3, \frac{-1+y}{2}\right) = (3,2)$$

 $\frac{-1+y}{2} = 2 \Rightarrow y = 5$

14. Find the co-ordinates of the points of trisection of the line segment joining the points A(1, -2) and B(-3, 4).

Ans :

Ans :

[Board Term-2, 2012 Set(34)]

Let $P(x_1, y_1), Q(x_2, y_2)$ divides AB into 3 equal parts. Thus P divides AB in the ratio of 1:2. As per question, line diagram is shown below.

Now

$$x_{1} = \frac{1(-3) + 2(1)}{1+3} = \frac{-3+2}{3} = \frac{-1}{3}$$
$$y_{1} = \frac{1(4) + 2(-2)}{1+2} = \frac{4-4}{3} = 0$$

Co-ordinates of P is $\left(-\frac{1}{3}, 0\right)$.

Here Q is mid-point of PB.

$$y_2 = \frac{0+4}{2} = 2$$

 $x_2 = \frac{-\frac{1}{3} + (-3)}{2} = \frac{-10}{6} = \frac{-5}{3}$

Thus co-ordinates of Q is $\left(-\frac{5}{2},2\right)$.

15. If (a, b) is the mid-point of the segment joining the points A(10, -6) and B(k, 4) and a - 2b = 18, find the value of k and the distance AB.

Ans :

[Board Term-2, 2012 Set(21)]

We have A(10, -6) and B(k, 4). If P(a, b) is mid-point of AB, then we have

$$(a, b) = \left(\frac{k+10}{2}, \frac{-6+4}{2}\right)$$

$$a, b = \begin{pmatrix} 2 & 2 \\ 2 & 2 \end{pmatrix}$$

 $a = \frac{k+10}{2}$ and $b = -1$

From given condition we have

$$a - 2b = 18$$

Substituting value b = -1 we obtain

$$a + 2 = 18 \Rightarrow a = 16$$

$$a = \frac{k + 10}{2} = 16 \Rightarrow k = 22$$

$$P(a, b) = (16, 1)$$

$$AB = \sqrt{(22 - 10)^2 + (4 + 6)^2}$$

 $=2\sqrt{61}$ units

16. Find the ratio in which the line 2x + 3y - 5 = 0 divides the line segment joining the points (8, -9) and (2,1). Also find the co-ordinates of the point of division.
Ans: [Board Term-2, 2012 Set(21)]

Let a point P(x, y) on line 2x + 3y - 5 = 0 divides AB in the ratio k:1.

 $x = \frac{2k+8}{k+1}$

 $y = \frac{k-9}{k+1}$

Now

and

Substituting above value in line 2x + 3y - 5 = 0 we have

$$2\left(\frac{2k+8}{k+1}\right) + 3\left(\frac{k-9}{k+1}\right) - 5 = 0$$

$$4k + 16 + 3k - 27 - 5k - 5 = 0$$

$$2k - 16 = 0$$

$$k = 8$$

Thus ratio is 8:1.

2

Substituting the value k = 8 we get

$$x = \left(\frac{2 \times 8 + 8}{8 + 1}\right) = \frac{8}{3}$$
$$y = \left(\frac{8 - 9}{8 + 1}\right) = -\frac{1}{9}$$
$$P(x, y) = \left(\frac{8}{3}, -\frac{1}{9}\right)$$

Thus

Ans :

Find the area of the rhombus of vertices (3,0),(4,5), (-1,4) and (-2,-1) taken in order.
 Ans : [Board Term-2, 2012 Set (40)]

We have
$$A(3,0), B(4,5), C(-1,4), D(-2,-1)$$

Diagonal AC , $d_1 = \sqrt{(3+1)^2 + (0-4)^2}$
 $= \sqrt{16+16} = \sqrt{32}$
 $= \sqrt{16 \times 2} = 4\sqrt{2}$
Diagonal BD , $d_2 = \sqrt{(4+2)^2 + (5+1)^2}$
 $= \sqrt{36+36} = \sqrt{72}$
 $= \sqrt{36 \times 2} = 6\sqrt{2}$
Area of rhombus $= \frac{1}{2} \times d_1 \times d_2$
 $= \frac{1}{2}4\sqrt{2} \times 6\sqrt{2}$
 $= 24$ sq. unit.

18. Find the ratio in which the line joining points (a+b,b+a) and (a-b,b-a) is divided by the point (a,b).

Let A(a+b,b+a), B(a-b,b-a) and P(a,b) and P divides AB in k:1, then we have

$$a = \frac{k(a-b) + 1(a+b)}{k+1}$$
$$a(k+1) = k(a-b) + a + b$$
$$ak + a = ak - bk + a + b$$
$$bk = b$$
$$k = 1$$

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Thus (a, b) divides A(a + b, b + a) and B(a - b, b - a)in 1:1 internally.

19. In what ratio does the point $\left(\frac{24}{11}, y\right)$ divides the line segment joining the points P(2, -2) and Q(3, 7)? Also find the value of y. [CBSE Marking Scheme, 2017]

As per question, line diagram is shown below.

$$P \vdash K \qquad 1 \qquad Q \\ (2,-2) \qquad \left(\frac{24}{11},y\right) \qquad (3,7)$$

Let $P(\frac{24}{11}, y)$ divides the segment joining the points P(2,-2) and Q(3,7) in ratio k:1.

Using intersection formula $x = \frac{mx_2 + nx_1}{m+1}$ we have

$$\frac{3k+2}{k+1} = \frac{24}{11}$$
$$33k+22 = 24k+24$$
$$9k = 2$$
$$k = \frac{2}{9}$$

Hence,

Ans :

Ans:

20. Find the co-ordinates of the points which divide the line segment joining the points (5,7) and (8,10) in 3 equal parts.

[Outside Delhi Compt. Set-II, 2017]

 $y = \frac{-18 + 14}{11} = -\frac{4}{11}$

Let $P(x_1, y_2)$ and $Q(x_2, y_2)$ trisect AB. Thus P divides AB in the ratio 1:2

As per question, line diagram is shown below.

$$(5,\overline{7}) \qquad \begin{array}{c|c} & & \\ P & & Q & (8,10) \end{array}$$

Now

$$y = \frac{1(10) + 2(7)}{3} = 8$$

 $x = \frac{1(8) + 2(7)}{3} = 6$

Thus $P(x_1, y_1)$ is P(6, 8). Since Q is the mid point of PB, we have

$$x_1 = \frac{6+8}{2} = 7$$
$$y_1 = \frac{8+10}{2} = 9$$

Thus $Q(x_2, y_2)$ is Q(7,9)

21. Find the co-ordinates of a point on the axis which is equidistant from the points A(2, -5) and B(-2, 9). Ans : [Delhi Compt. Set-I, 2017]

Let the point P on the x axis be (x,0). Since it is equidistant from the given points A(2, -5) and B(-2,9)

$$PA = PB$$

$$PA^{2} = PB^{2}$$

$$(x-2)^{2} + [0 - (-5)]^{2} = (x - (-2))^{2} + (0 - 9)^{2}$$

$$x^{2} - 4x + 4 + 25 = x^{2} + 4x + 4 + 81$$

$$-4x + 29 = 4x + 85$$

$$x = -\frac{56}{8} = -7$$

Hence the point on x axis is (-7, 0)

22. The line segment joining the points A(3, -4) and B(1,2) is trisected at the points P and Q. Find the coordinate of the PQ.

Let $P(x_1, y_1)$ and $Q(x_2, y_2)$ trisect AB. Thus P divides AB in the ratio 1:2

As per question, line diagram is shown below.

Using intersection formula

Ans :

$$x = \frac{1 \times 1 + 2 \times 3}{1 + 2} = \frac{7}{3}$$
$$y = \frac{1 \times 2 + 2 \times -4}{1 + 2} = -2$$

Hence point P is $\left(\frac{7}{3}, -2\right)$

23. Show that $\triangle ABC$ with vertices A(-2,0), B(0,2)and C(2,0) is similar to ΔDEF with vertices D(-4,0), F(4,0) and E(0,4).

Ans: [Board Foreign Set-I, II 2017], [Delhi Board Set-I, II, II, II 2017]

Using distance formula

$$AB = \sqrt{(0+2)^2 + (2-0)^2} = \sqrt{4+4}$$

= $2\sqrt{2}$ units
$$BC = \sqrt{(2-0)^2 + (0-2)^2} = \sqrt{4+4}$$

= $2\sqrt{2}$ units
$$CA = \sqrt{(-2, -2)^2 + (0-0)^2} = \sqrt{16}$$

= 4 units
and
$$DE = \sqrt{(0+4)^2 + (4-0)^2} = \sqrt{32}$$

= $4\sqrt{2}$ units
$$EF = \sqrt{(4-0)^2 + (0-4)^2} = \sqrt{32}$$

= $4\sqrt{2}$ units
$$FD = \sqrt{(-4-4)^2 + (0-0)^2} = \sqrt{64}$$

= 8 units
$$\frac{AB}{DE} = \frac{BC}{EF} = \frac{AC}{DF}$$

$$\frac{2\sqrt{2}}{4\sqrt{2}} = \frac{2\sqrt{2}}{4\sqrt{2}} = \frac{4}{8} = \frac{1}{2}$$

Since Ratio of the corresponding sides of two similar Δs is equal, we have

> $\Delta ABC \sim \Delta DEF$ Hence Proved.

24. Find the co-ordinates of the point on the y-axis which is equidistant from the points A(5,3) and B(1,-5)[Delhi Compt. Set-III, 2017] Ans : Let the points on y-axis be P(0, y)

Now
$$PA = PB$$

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Ans:

And

$$PA^{2} = PB^{2}$$

$$(0-5)^{2} + (y-3)^{2} = (0-1)^{2} + (y+5)^{2}$$

$$5^{2} + y^{2} - 6y + 9 = 1 + y^{2} + 10y + 25$$

$$16y = 8$$

$$y = \frac{1}{2}$$
Hence point on y-axis is $(0, \frac{1}{2})$.

25. In the given figure ΔABC is an equilateral triangle of side 3 units. Find the co-ordinates of the other two vertices.

The co-ordinates of B will be (2+3,0) or (5,0)Let co-ordinates of C be (x,y)

Since triangle is equilateral, we have

$$A C^{2} = BC^{2}$$

$$(x-2)^{2} (y-0)^{2} = (x-5)^{2} + (y-0)^{2}$$

$$x^{2} + 4 - 4x + y^{2} = x^{2} + 25 - 10x + y^{2}$$

$$6x = 21$$

$$x = \frac{7}{2}$$

$$(x-2)^{2} + (y-0)^{2} = 9$$

$$\left(\frac{7}{2} - 2\right)^{2} + y^{2} = 9$$

$$\frac{9}{4} + y^{2} = 9 \text{ or, } y^{2} = 9 - \frac{9}{4}$$

 $y^2 = \frac{27}{4} = \frac{3\sqrt{3}}{2}$ Hence *C* is $\left(\frac{4}{3}, \frac{3\sqrt{3}}{2}\right)$.

26. Find the co-ordinates of the points of trisection of the line segment joining the points (3, -2) and (-3, -4).
Ans: [Board Foreign Set-I, II, III 2017]

Let $P(x_1, y_1)$ and $Q(x_2, y_2)$ trisect the line joining A(3, -2) and B(-3, -4).

As per question, line diagram is shown below.

Thus P divides AB in the ratio 1:2

Using intersection formula $x = \frac{mx_2 + nx_1}{m + n}$ and $y = \frac{my_2 + my_1}{m + n}$

$$x_1 = \frac{1(-3) + 2(3)}{1+2} = 1$$

 $y_1 = \frac{1(-4) + 2(-2)}{1+2} = -\frac{8}{3}$

and

Thus we have x = 1 and $y = -\frac{8}{3}$

Since Q is at the mid-point of PB, using mid-point formula

$$x_{2} = \frac{1-3}{2} = -1$$
$$y_{2} = \frac{-\frac{8}{3} + (-4)}{2} = -\frac{10}{3}$$

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Hence the co-ordinates of P and Q are $(1, -\frac{8}{3})$ and $(-1, -\frac{10}{3})$

27. If the distances of P(x, y) from A(5, 1) and B(-1, 5) are equal, then prove that 3x = 2y.

[Outside Delhi, Set-II, 2016]

Since P(x, y) is equidistant from the given points A(5, 1) and B(-1, 5),

$$PA = PB$$
$$PA^2 = PB^2$$

Using distance formula,

Ans:

$$(5-x)^{2} + (1-y)^{2} = (-1-x)^{2} + (5-y)^{2}$$

$$(5-x)^{2} + (1-y)^{2} = (1+x)^{2} + (5-y)^{2}$$

$$25-10x+1-2y = 1+2x+25-10y$$

$$-10x-2y = 2x-10y$$

$$8y = 12x$$

$$3x = 2y$$
Hence proved.

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LONG ANSWER TYPE QUESTIONS

1. If P(9a-2, -b) divides the line segment joining A(3a+1, -3) and B(8x, 5) in the ratio 3:1. Find the values of a and b.

Ans :

[Board Sample Paper, 2016]

Using section formula we have

$$9a - 2 = \frac{3(8a) + 1 + (3a + 1)}{3 + 1} \qquad \dots (1)$$

$$-b = \frac{3(5) + 1(-3)}{3+1} \qquad \dots (2)$$

Form (2)
$$-b = \frac{15-3}{4} = 3 \Rightarrow b = -3$$

From (1),
$$9a-2 = \frac{24a+3a+1}{4}$$

$$4(9a-2) = 27a + 1$$
$$36a - 8 = 27a + 1$$
$$9a = 9$$
$$a = 1$$

2. Find the coordinates of the point which divide the line segment joining A(2, -3) and B(-4, -6) into three

and

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equal parts.

Ans :

[Board Sample paper, 2016]

Let $P(x_1, y_1)$ and $Q(x_2, y_2)$ trisect the line joining A(3, -2) and B(-3, -4).

As per question, line diagram is shown below.

P divides AB in the ratio of 1:2 and Q divides ABin the ratio 2:1.

By section formula

$$x_{1} = \frac{mx_{2} + nx_{1}}{1+2} \text{ and } y = \frac{my_{2} + ny_{1}}{m+n}$$

$$P(x_{1}, y_{1}) = \left(\frac{1(-4) + 2(2)}{2+1}, \frac{2(-6) + 1(-3)}{2+1}\right)$$

$$= \left(\frac{-4 + 4}{3}, \frac{-6 - (-6)}{3}\right)$$

$$= (0, -4)$$

$$Q(x_{2}, y_{2}) = \left(\frac{2(-4) + 1(2)}{2+1}, \frac{2(-6) + 1(-3)}{2+1}\right)$$

$$= \left(\frac{-8 + 2}{3}, -\frac{12 + (-3)}{3}\right) = (-2, -5)$$

The base BC of an equilateral triangle ABC lies on 3. y-axis. The co-ordinates of point C are (0,3). The origin is the mid-point of the base. Find the coordinates of the point A and B. Also find the coordinates of another point D such that BACD is a rhombus.

Ans : [Foreign Set I, II, 2015]

As per question, diagram of rhombus is shown below.



$$\begin{array}{rcl} + 9 &= 36 \\ x^2 &= 27 \Rightarrow x = \pm 3\sqrt{3} \end{array}$$

(0, -3)

Co-ordinates of point A is $(3\sqrt{3},0)$

Since ABCD is a rhombus

$$AB = AC = CD = DB$$

Thus co-ordinate of point D is $(-3\sqrt{3},0)$

The base QR of an equilateral triangle PQR lies on 4.

x-axis. The co-ordinates of point Q are (-4,0) and the origin is the mid-point of the base. find the coordinates of the point P and R. Ans:

[Foreign set III, 2015]

As per question, line diagram is shown below.



Co-ordinates of point R is (4,0)Thus QR = 8 units Let the co-ordinates of point P be (0, y)Since PQ = QR $(-4-0)^2 + (0-y)^2 = 64$ $16 + y^2 = 64$ $y = \pm 4\sqrt{3}$ Coordinates of P are $(0, 4\sqrt{3})$ or $(0, -4\sqrt{3})$

TOPIC 2: AREA OF TRIANGLE

VERY SHORT ANSWER TYPE QUESTIONS

Find the area of the triangle with vertices (0,0)(6,0)1. and (0,5)

[Board Term-2, 2015]

Ans :

$$\Delta = \frac{1}{2} [x_1(y_2 - y_3) + x_2(y_3 - y_1) + x_3(y_1 - y_2)]$$

= $\frac{1}{2} [0(0 - 5) + 6(5 - 0) + 0(0 - 0)]$
= $\frac{1}{2} [6 \times 5] = 15$ sq. units

If the points A(x,2), B(-3, -4), C(7, -5) are collinear, 2. then find the value of x.

Since the points are collinear, then

Area of triangle = 0

$$\frac{1}{2}[x_1(y_2 - y_3) + x_2(y_3 - y_1) + x_3(y_1 - y_2)] = 0$$

$$[x(-4+5) + (-3)(-5-2) + 7(2+4)] = 0$$

$$x + 21 + 42 = 0$$

$$x = -63$$

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3. In Fig., find the area of triangle ABC (in sq. units)?



Ans :

[Board Term-2, 2013]

Area of triangle

$$\Delta = \frac{1}{2} [x_1(y_2 - y_3) + x_2(y_3 - y_1) + x_3(y_1 - y_2)]$$

= $\frac{1}{2} [1(0 - 0) + (-1)(0 - 3) + 4(3 - 0)]$
= $\frac{1}{2} [2 + 12] = \frac{15}{2} = 7.5$ s, units

4. If the point (0,0),(1,2) and (x,y) are collinear, then find x.

Ans : [Board Term-2, 2011, Set A1]

The points are collinear, then area of triangle must be zero.

$$\frac{1}{2}[x_1(y_2 - y_3) + x_2(y_3 - y_1) + x_3(y_1 - y_2)] = 0$$
$$[0(2 - y) + 1(y - 0) + x(0 - 2)] = 0$$
$$[y - 2x] = 0$$
$$x = \frac{y}{2}$$

SHORT ANSWER TYPE QUESTIONS - I

1. Show that the points A(0,1), B(2,3) and C(3,4) are collinear.

Ans :

[CBSE Term-2, 2016 Set-HODM4OL]

If the area of the triangle formed by the points is zero, then points are collinear.

We have A(0,1), B(2,3) and C(3,4)

$$\Delta = \frac{1}{2} |0(3-4) + 2(4-1) + 3(1-3)|$$

= $\frac{1}{2} |0 + (2)(3) + (3)(-2)||$
= $\frac{1}{2} |6-6| = 0$

Thus given points are collinear.

2. Prove that the points (2, -2), (-2, 1) and (5, 2) are the vertices of a right angled triangle. Also find the area of this triangle.

Ans : [Foreign Set I, II, III, 2016]

We have A(2, -2), B(-2, 1) and (5, 2)

Applying distance formula we get

$$AB^{2} = (2+2)^{2} + (-2-1)^{2}$$

= 16 + 9 = 25
Thus $AB = 5$
Similarly $AC^{2} = (-2-5)^{2} + (1-2)^{2}$
= 49 + 1 = 50
 $BC^{2} = 50 \Rightarrow BC = 5\sqrt{2}$
 $AC^{2} = (2-5)^{2} + (-2-2)^{2}$
= 9 + 16
= 25
 $AC^{2} = 25 \Rightarrow AC = 5$
Clearly $AB^{2} + AC^{2} = BC^{2}$
 $25 + 25 = 50$

Hence the triangle is right angled,

А

Ans :

Ans :

rea of
$$\triangle ABC = \frac{1}{2} \times Base \times Height$$

= $\frac{1}{2} \times 5 \times 5 = \frac{25}{2} sq. unit.$

3. Find the relation between x and y, if the point A(x,y), B(-5,7) and C(-4,5) are collinear.

Ans : [Outside Delhi CBSE Board, 2015, Set I, II, III] If the area of the triangle formed by the points is zero,

If the area of the triangle formed by the points is zero, then points are collinear.

$$\frac{1}{2}[x_1(y_2 - y_3) + x_2(y_3 - y_1) + x_3(y_1 - y_2)] = 0$$
$$[x(7 - 5) - 5(5 - y) - 4(y - 7)] = 0$$
$$2x - 25 + 5y - 4y + 28 = 0$$
$$2x + y + 3 = 0$$

4. For what values of k are the points (8,1), (3, -2k)and (k, -5) collinear?

[Foreign Set I, II, III 2015]

Since points (8,1), (3, -2k) and (k, -5) are collinear, area of triangle formed must be zero.

$$\frac{1}{2} \Big[8(-2k+5) + 3(-5,-1) + k(1+2k) \Big] = 0$$
$$2k^2 - 15k + 22 = 0$$
$$k = 2, \frac{11}{2}$$

SHORT ANSWER TYPE QUESTIONS - II

1. Find the value of p, if the points A(2,3), B(4,p), C(6,-3) are collinear.

[Baord Term-2, 2012 sEt (17)]

Since points A(2,3), B(4,p) and C(6, -3) are collinear, area of triangle formed must be zero.

$$\frac{1}{2}[x_1(y_2 - y_3) + x_2(y_3 - y_1) + x_3(y_1 - y_2)] = 0$$
$$[2(p+3) + 4(-3-3) + 6(3-p)] = 0$$

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Ans :

$$[2p + 6 - 24 + 18 - 6p] = 0$$
$$[-4p] = 0$$
$$4p = 0$$
$$p = 0$$

2. If (5,2),(-3,4) and (x,y) are collinear, show that x+4y-13=0

[CBSE Board Term-2, 2015]

Since points (5,2),(-3,4) and (x,y) are collinear, area of triangle formed must be zero.

$$\frac{1}{2}[x_1(y_2 - y_3) + x_2(y_3 - y_1) + x_3(y_1 - y_2)] = 0$$

$$[5(4 - y) + (-3)(y - 2) + x(2 - 4)] = 0$$

$$[20 - 5y - 3y + 6 + (-2x)] = 0$$

$$[-2x - 8y + 26] = 0$$

$$x + 4y - 13 = 0$$

Hence proved

3. Find the area of a triangle ABC with A(1, -4) and mid-points of sides through A being (2, -1) and (0, -1).

Ans: [Delhi CBSE Board, 2015, Set I, III]

Let $B(x_1, y_1)$ and $C(x_2, y_2)$ be other vertices of triangle. As per question, triangle is shown below.



Let E(2, -1) be the mid point of AB and F(0, -1) be the mid point of AC.

 $\frac{x_1+1}{2} = 2 \implies x_1 = 3$

Now

and $\frac{y_1 + (-4)}{2} = -1 \Rightarrow y_2 = 2$

Thus point B is (3, 2).

Again

$$\frac{y_2 + (-4)}{2} = -1 \Rightarrow y_1 = 2$$

 $\frac{x_2-1}{2} = 0 \Rightarrow x_1 = -1$

Thus point C is (-1,2)

Now the co-ordinates are A(1, -4), B(3, 2), C(-1, 2)Area of triangle

$$\Delta = \frac{1}{2} [x_1(y_2 - y_3) + x_2(y_3 - y_1) + x_3(y_1 - y_2)]$$
$$= \frac{1}{2} [1(2-2) + 3(2+4) - 1(-4-2)]$$

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$$=\frac{1}{2}[0+18+6] = 12$$
 sq. units

4. Find the area of the triangle PQR with Q(3,2) and mid-points of the sides through Q being (2, -1) and (1,2).

[Delhi CBSE Board, 2015 Set III]

Let $P(x_1, y_1)$ and $Q(x_2, y_2)$ be other vertices of triangle. As per question, triangle is shown below.



Let D(2, -1) be the mid point of PQ and E(1, 2) be the mid point of AC.

Let the co-ordinate of p be (x, y) and $R(x_1, y_1)$

 $\frac{x_1+3}{2} = 2 \implies x_1 = 1$

Ans :

 $\frac{y_1+2}{2} = -1 \Rightarrow y_2 = -4$

Thus point is P(1, -4)

Again

Ans:

ain

 $\frac{y_2+2}{2} = 2 \Rightarrow y_1 = 2$

 $\frac{x_2+3}{2} = 1 \Rightarrow x_1 = -1$

Thus point is R(-1,2)Now we have P(1, -4), Q(3,2), R(-1,2)Area of triangle

$$\Delta = \frac{1}{2} [x_1(y_2 - y_3) + x_2(y_3 - y_1) + x_3(y_1 - y_2)]$$

= $\frac{1}{2} [1(2-2) + 3(2+4) + (-1)(-4-2)]$
= $\frac{1}{2} [0 + 18 + 6] = \frac{1}{2} \times 24 = 12$ sq. units

5. If the points A(-2,1), B(a,b) and C(4,1) are collinear and a-b=1, find a and b.

b = 1

If three points are collinear, then area covered by given points must be zero. Thus area

$$\frac{1}{2} [x_1(y_2 - y_3) + x_2(y_3 - y_1) + x_3(y_1 - y_2)] = 0$$
$$\frac{1}{2} [-2(b-1) + a(1-1) + 4(1-b)] = 0$$
$$[-2b + 2 + 0 + 4(1-b)] = 0$$
$$-6b + 6 = 0 \Rightarrow$$

Substituting b = 1 in given condition a - b = 1 we

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have

$$\begin{array}{c} a-1 \ = 1 \\ a \ = 2 \end{array}$$

This a = 2 and b = 1.

- 6. Find the area of the quadrilateral ABCD, the coordinates of whose vertices are A(5, -2), B(-3, -1), C(2, 1) and D(6, 0).
 - Ans: [Delhi Set, 2014], [Board Term-2, 2012 set (13)]

As per question the quadrilateral ABCD is shown below.



Area of quadrilateral

$$= \Delta_{ABC} + \Delta_{ADC}$$

$$ABCD = ar(\Delta ABC) + ar(ADC)$$

$$Area_{ABCD} = \frac{1}{2}[(x_1y_2 - x_2y_1) + (x_2y_3 - x_3y_2)]$$

$$+ (x_3y_4 - x_4y_3) + (x_4y_1 - x_1y_4)$$

$$= \frac{1}{2}[5(-1) - (-2)(-3) + (-3)(1)$$

$$- (-1)(2) + (2 \times 0 - 1 \times 6) + 6(-2) - (0 \times 5)$$

$$= \frac{1}{2}[-30] = |-15| = 15 \text{ sq. units}$$

7. In the given triangle ABC as shown in the diagram D, E and F are the mid-points of AB, BC and AC respectively. Find the area of ΔDEF .



 $x_D = \frac{3+-5}{2} = -1$

 $y_D = \frac{2-6}{2} = -2$

Ans :

Mid-point $B\!A$

[Board Term-2, 2012 Set (5)]

and

Thus point D is (-1, -2)Mid-point BC, $x_E = \frac{-5+7}{2} = 1$ and $y_E \frac{-6+4}{2} = -1$ Thus point is E is (1, -1).

Mid-Point *CA*,
$$x_F = \frac{7+3}{2} = 5$$

 $y_F = \frac{4+2}{2} = 3$

Thus point F is (5,3)Now, area ΔDEF

$$\Delta = \frac{1}{2} [-(-1-3) + 1(3+2) + 5(-2+1)]$$
$$= \frac{1}{2} [4+5-5]$$

= 2 Unit

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8. Find the area of the triangle formed by joining the midpoints of the sides of a triangle, whose co-ordinates of vertices are (0, -1), (2, 1) and (0, 3).

Let the vertices of given triangle be A(0, -1), B(2, 1)and C(0,3). As per question the triangle is shown below.

Let the coordinates of mid-points

$$P = \left(\frac{0+2}{2}, \frac{-1+1}{2}\right) = (1,0)$$
$$Q = \left(\frac{2+0}{2}, \frac{1+3}{2}\right) = (1,2)$$
$$Q = \left(\frac{0+0}{2}, \frac{-1+3}{2}\right) = (0,1)$$
Area of ΔPQR

$$\Delta = \frac{1}{2} [x_1(y_2 - y_1) + x_2(y_3 - y_1) + x_3(y_1 - y_2)]$$

= $\frac{1}{2} [(2 - 1) + 1(1 - 0) + 0(0 - 2)]$
= $\frac{1}{2} (1 + 1 + 0) = 1$ sq. units

9. The area of a triangle is 5 sq. units. Two of its vertices are (2,1) and (3, -2). If the third vertex is $(\frac{7}{2}, y)$, Find the value of y.

Ans: [Delhi Set II 2017]

We have $\Delta ABC = 5$ sq. units

 $\frac{1}{2}$

$$\begin{bmatrix} 2(-2-y) + (y-1) + \frac{7}{2}(1+2) \end{bmatrix} = 5$$
$$\frac{1}{2} \begin{bmatrix} -4 - 2y + 3y - 3 + \frac{21}{2} \end{bmatrix} = 5$$
$$y + \frac{7}{2} = 10$$
$$y = 10 - \frac{7}{2} = \frac{13}{2}$$

If we consider possibility of negative area then, we have

$$y + \frac{7}{2} = -10$$
$$y = -10 - \frac{7}{2} = -\frac{27}{2}$$

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Hence the value of
$$y$$
 is $\frac{13}{2}$ or $-\frac{27}{2}$

LONG ANSWER TYPE QUESTIONS

1. Prove that the area of a triangle with vertices (t, t-2), (t+2, t+2) and (t+3) is independent of t. Ans: [Delhi Set I, II, III, 2016]

Area of the triangle

$$\Delta = \frac{1}{2} |t(t+2-t) + (t+2)(t-t+2) + (t+3)(t-2-t-2)|$$
$$= \frac{1}{2} [2t+2t+4-4t-12]$$

= 4 sq. units. which is independent of t.

2. Find the area of a quadrilateral ABCD, the coordinates of whose vertices are A(-3,2), B(5,4), C(7,-6) and D(-5,-4). Ans: [Foreign Set III, 2016]

As per question the quadrilateral is shown below.



Area of triangle ABD

$$\Delta_{ABD} = \frac{1}{2} |-3(8) + 5(-6) + -5(2-4)|$$

= 22 sq. units

Area of triangle BCD

Ans :

$$\Delta_{BCD} = \frac{1}{2} \left| 5(-2) + 7(-8) - 5(10) \right|$$

= 58 sq. units $\text{Area}_{ABCD} = \Delta_{ABD} + \Delta_{BCD}$

$$= 22 + 58 = 80$$
 sq. units

3. If A(-4,8), B(-3,-4), C(0,-5) and D(5,6) are the vertices of a quadrilateral *ABCD*, find its area.

[Delhi CBSE Board, 2015 Set I, III]

We have A(-4,8), B(-3,-4), C(0,5) and D(5,6)Area of quadrilateral

$$= \frac{1}{2} [(x_1 y_2 - x_2 y_1) + (x_2 y_3 - x_3 y_2) + (x_3 y_4 - x_4 y_3) + (x_4 y_1 - x_1 y_4)]$$

Area
$$= \frac{1}{2} [\{-4 \times (-4) - (-3)(8)\} + \{(-3)(-5) - 0 \times (-4)\} + \{0 \times 6 - 5(-5)\} + [\{5 \times 8 - (-4)(6)\}]$$
$$= \frac{1}{2} [16 + 24 + 15 - 0 + 0 + 25 + 40 + 24]$$

$$= \frac{1}{2} [40 + 15 + 25 + 40 + 24] = \frac{1}{2} \times 144 = 72$$
 sq. units

4. If
$$P(-5, -3)$$
, $Q(-4, -6)$, $R(2, -3)$ and $S(1, 2)$ are the
vertices of a quadrilateral *PQRS*, find its area.
Ans: [Delhi CBSE Board, 2015 Set II]
We have $P(-5, -3)$, $Q(-4, -6)$, $R(2, -3)$ and $S(1, 2)$
Area of quadrilateral
 $= \frac{1}{2}[(x_1y_2 - x_2y_1) + (x_2y_3 - x_3y_2) + (x_3y_4 - x_4y_3) + (x_4y_1 - x_1y_4)]$
Area
 $= \frac{1}{2}[-5(-6) - (-4)(-3) + (-4)(-3) - 2(-6)$

$$+(2)(2) - 1 \times (-3) + 1 \times (-3) - (-5)(2)]$$

= $\frac{1}{2}[30 - 12 + 12 + 12 + 4 + 3 - 3 + 10]$
= $\frac{1}{2}[30 + 12 + 4 + 10] = \frac{1}{2}[56] = 28$ sq. units

5. Find the values of k so that the area of the triangle with vertices (1, -1), (-4, 2k) and (-k, -5) is 24 sq. units.

Ans : [Outside Delhi CBSE Board, 2015, Set I] We have (1, -1), (-4, 2k) and (-k, -5)Area of triangle

$$\Delta = \frac{1}{2} [x_1(y_2 - y_3) + x_2(y_3 - y_1) + x_3(y_1 - y_2)]$$

$$24 = \frac{1}{2} [1(2k+5) - 4(-5+1) - k(-1-2k)]$$

$$48 = 2k+5+16+k+2k^2$$

$$2k^2 + 3k - 27 = 0$$

$$(k-3)(2k+9) = 0$$

$$k = 3, -\frac{9}{2}$$

6. Find the values of k so that the area of the triangle with vertices (k+1,1), (4,-3) and (7,-k) is 6 sq. units.

[Outside Delhi CBSE Board, 2015, Set I]

We have (k+1,1), (4,-3) and (7,-k)Area of triangle

Ans :

$$\Delta = \frac{1}{2} [x_1(y_2 - y_3) + x_2(y_3 - y_1) + x_3(y_1 - y_2)]$$

$$6 = \frac{1}{2} [(k+1)(-3+k) + 4(-k-1) + 7(1+3)]$$

$$12 = [k^{2} - 2k - 3 - 4k - 4 + 28]$$

$$12 = k^{2} - 6k + 21$$

$$k^{2} - 6k + 9 = 0$$

$$(k - 3)(k - 3) = 0$$

$$k = 3, 3$$

given points must be zero.

7. Find the values of k for which the points A(k+1, 2k), B(3k, 2k+3) and C(5k-1, 5k) are collinear. Ans: [Outside Delhi CBSE Board, 2015, Set III] If three points are collinear, then area covered by

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Ans :

Diagonal

$$= \frac{1}{2} [x_1(y_2 - y_3) + x_2(y_3 - y_1) + x_3(y_1 - y_2)] = 0$$

$$[x_1(y_2 - y_3) + x_2(y_3 - y_1) + x_3(y_1 - y_2)] = 0$$

$$[(k+1)(2k+3-5k) + 3k(5k-2k) + (5k-1)(2k-2k-3) = 0$$

$$-3k^2 + 3k - 3k + 3 + 9k^2 - 15k + 3 = 0 = 0$$

$$6k^2 - 15k + 6 = 0$$

$$2k^2 - 5k + 2 = 0$$

$$(k-2)(2k-1) = 0$$
Thus $k = 2$ or $k = \frac{1}{2}$

8. The vertices of quadrilateral ABCD are A(5, -1), B(8,3), C(4,0) and D(1, -4). Prove that ABCD is a rhombus.

[Board Term-2, 2015]

The vertices of the quadrilateral *ABCD* are

$$A(5, -1), B(8, 3), C(4, 0) D(1, -4).$$

Now
 $AB = \sqrt{(8-5)^2 + (3+1)^2}$
 $= \sqrt{3^2 + 4^2} = 5$ units
 $BC = \sqrt{(8-4)^2 + (3-0)^2}$
 $= \sqrt{4^2 + 3^2} = 5$ units
 $CD = \sqrt{(4-1)^2 + (0+4)^2}$
 $= \sqrt{(3)^2 + (4)^2} = 5$ units
 $AD = \sqrt{(5-1)^2 + (-1+4)^2}$
 $= \sqrt{(4)^2 + (3)^2} = 5$ units
Diagonal,
 $AC = \sqrt{(5-4)^2 + (-1-0)^2}$
 $= \sqrt{1^2 + 1^2} = \sqrt{2}$ units

$$= \sqrt{1^{2} + 1^{2}} = \sqrt{2} \text{ units}$$

BD = $\sqrt{(8 - 1)^{2} + (3 + 4)^{2}}$
= $\sqrt{(7)^{2} + (7)^{2}} = 7\sqrt{2} \text{ units}$

As the length of all the sides are equal but the length of the diagonals are not equal. Thus ABCD is not square but a rhombus.

9. A(4, -6), B(3, -2) and C(5,2) are the vertices of a ΔABC and AD is its median. Prove that the median AD divides ΔABC into two triangles or equal areas.
Ans : [CBSE 0.D. 2014]

Since AD is the median of ΔABC from vertex A, we have

$$D(x,y) = \left(\frac{3+5}{2} + \frac{-2+2}{2}\right) = (4,0)$$

As per question statement triangle is shown below.



Area of ΔADB ,

$$\Delta_{\text{ADB}} = \frac{1}{2} \times (4(0+2) + (-2+6) + 3(-6-0))$$

$$= \frac{1}{2} \times (8 + 16 + -18)$$
$$= \frac{1}{2} \times 3 = 3 \text{ square units}$$
(1)

Area of ΔACB

$$\Delta_{ACB} = \frac{1}{2} \times (4(0-2) + 4(2+6) + 5(-6-0))$$
$$= \frac{1}{2} \times (-8 + 32 - 30)$$
$$= \frac{1}{2} \times -6 = -3$$

Since area can not be negative, we take positive value.

Thus $\Delta_{ACB} = 3$ square units (2) From (1) and (2) we seen that $\Delta_{ADB} = \Delta_{ACB}$. It is verified that median of ΔABC divides it into two triangles of equal areas.

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10. The co-ordinates of vertices of $\triangle ABC$ are A(0,0), B(0,2) and C(2,0). Prove that $\triangle ABC$ is an isosceles triangle. Also find its area. Ans:

Ans: [Board Term-2, 2014]
Using distance formula
$$d = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$
 we have

$$AB = \sqrt{(0-0)^2 + (0-2)^2} = \sqrt{4} = 2$$

$$AC = \sqrt{(0-2)^2 + (0-0)^2} = \sqrt{4} = 2$$

$$BC = \sqrt{(0-2)^2 + (2-0)^2} = \sqrt{4+4} = 2\sqrt{2}$$

Clearly, $AB = AC \neq BC$

Ans :

Thus ΔABC is an isosceles Triangle

Now,
$$AB^2 + AC^2 = 2^2 + 2^2 = 4 + 4 = 8$$

also, $BC^2 = (2\sqrt{2})^2 = 8$
 $AB^2 + AC^2 = BC^2$

Thus ΔABC is an isosceles right angled triangle. Now, area of ΔABC

$$\Delta_{ABC} = \frac{1}{2}base \times height$$
$$= \frac{1}{2} \times 2 \times 2$$
$$= 2 \text{ sq. units.}$$

11. Find the area of the quadrilateral PQRS. The coordinates of whose vertices are P(-4, -2), Q(-3, -5), R(3, -2) and 5(2, 3).

[Outside Delhi Set-II, 2017]

As per question quadrilateral PQRS is shown below.



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Area
$$\Box_{PQRS} = \Delta_{PQR} + \Delta_{PRS}$$

Area ΔPQR
 $\Delta_{PQR} = \frac{1}{2} [x_1(y_2 - y_1) + x_2(y_3 - y_1) + x_2(y_1 - y_2)]$
 $= \frac{1}{2} [-4(-2 - (-5)) + 3(-5 - (-2)) + -3(-2 - (-2))]$
 $= \frac{1}{2} [-4 \times 3 + 3 \times -3 + 3 \times 0]$
 $= \frac{1}{2} \times (12 + 9) = \frac{21}{2}$ sq. units
Area ΔPRS
 $\Delta_{PRS} = \frac{1}{2} [-4(-2 - 3) + 3(3 + 2) + 2(-2 + 2)]$
 $= \frac{1}{2} [-4 \times -5 + 3 \times 5 + 0]$
 $= \frac{1}{2} \times (20 + 15) = \frac{35}{2}$ sq. units
Area $\Box_{PQRS} = \frac{21}{2} + \frac{35}{2} = 28$ sq. units

12. If the co-ordinates of two points are A(3,4), B(5,-2)and a point P(x,5) is such that PA = PB then find the area of ΔPAB .

[Outside Delhi Compt. Set-I, 2017]

Ans :

PA = PBSince

 $PA^2 = PB^2$

Using distance formula we have

$$(x-3)^{2} + (5-4)^{2} = (x-5)^{2} + (5+2)^{2}$$
$$x^{2} - 6x + 9 + 1 = x^{2} - 10x + 25 + 49$$
$$10x - 6x = 74 - 10$$
$$x = 16$$

Thus area ΔPAB

$$\Delta_{PAB} = \frac{1}{2} [16(4+2) + 3(-2-5) + 5(5-4)]$$
$$= \frac{1}{2} [96 - 21 + 5] = 40$$

Hence, area of triangle is 40 sq. units

13. Find the area of a quadrilateral PQRS whose vertices are P(4,3), Q(10, -1), R(15, 4) and S(10, 23). [Delhi Compt. Set III 2017] Ans :

As per question quadrilateral PQRS is shown below.



Area
$$\Box_{PQRS} = \Delta_{PQR} + \Delta_{PRS}$$

Area ΔPQR

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$$\Delta_{PQR} = \frac{1}{2} [x_1(y_2 - y_1) + x_2(y_3 - y_1) + x_2(y_1 - y_2)]$$
$$= \frac{1}{2} [4(-5) + 10(1) + 15(4)]$$
$$= \frac{1}{2} \times 50 = 25 \text{ sq. units}$$

Area ΔPRS

$$\Delta_{PRS} = \frac{1}{2} [4(-19) + 15(20) + 10(-1)]$$
$$= \frac{1}{2} \times 214 = 107 \text{ sq. units}$$
Area $\Box_{PQRS} = 25 + 107 = 132 \text{ sq. unit}$

14. Find the area of a quadrilateral ABCD, whose vertices are A(1,1), B(7, -3), C(12, 2) and D(7, 21).

[Delhi Compt. Set I 2017] Ans :

As per question quadrilateral ABCD is shown below.



Area of quadrilateral ABCD

$$\Box_{ABCD} = \Delta_{ABD} + \Delta_{BCD}$$

Area ΔABD ,

$$\Delta_{ABD} = \frac{1}{2} [1(-3-21) + 7(21-1) + 7(1+3)]$$
$$= \frac{1}{2} [-24 + 7 \times 20 + 7 \times 4]$$
$$= \frac{1}{2} [-24 + 140 + 28]$$
$$= \frac{1}{2} \times 144 = 72 \text{ sq. units}$$

Area ΔBCD ,

$$\Delta_{BCD} = \frac{1}{2} [7(2-21) + 12(21+3) + 7(-3-2)]$$

= $\frac{1}{2} [7 \times -19 + 12 \times 24 + 7 \times -5]$
= $\frac{1}{2} [-133 + 288 - 35]$
= $\frac{1}{2} [288 - 168]$
= $\frac{1}{2} \times 120 = 60$ sq. units

Area $\square_{ABCD} = 72 + 60 = 132$ sq. units.

15. Find the area of a quadrilateral PQRS whose vertices

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area P(-5,7), R(-1,-6) and S(4,5)Ans : [Delhi Compt. Set II, 2017]

As per question quadrilateral PQRS is shown below.



Area $\Box_{PQRS} = \Delta_{PQR} + \Delta_{QRS}$

Area ΔPQR

$$\Delta_{PQR} = \frac{1}{2} [x_1(y_2 - y_1) + x_2(y_3 - y_1) + x_2(y_1 - y_2)]$$

= $\frac{1}{2} [-5(-5-5) + -4(5-7) + 4(7+5)]$
= $\frac{1}{2} [50 + 8 + 48]$
= $\frac{1}{2} \times 106 = 53$ sq. units.

Area $\Delta \, QRS$

$$\Delta_{QRS} = \frac{1}{2} \left[-4(-6-5) + -1(5+5) + 4(-5+6) \right]$$
$$= \frac{1}{2} \left[44 + (-10) + 4 \right]$$
$$= \frac{1}{2} \times 38 = 19 \text{ sq. units}$$

Area

 $\Box_{PQRS} = 53 + 19 = 72$ sq. units

16. Find the area of the quadrilateral whose vertices are A(3,1), B(8,1), C(7,2) and D(5,3)

Ans: [Delhi Compt. Set II 2017]

As per question quadrilateral ABCD is shown below.



Area of quadrilateral ABCD

$$\Box_{ABCD} = \Delta_{ABC} + \Delta_{ACD}$$
Area of triangle

$$\Delta = \frac{1}{2} [x_1(y_2 - y_3) + x_2(y_3 - y_1) + x_2(y_1 - y_2)]$$

Area ΔABC

$$\Delta_{ABC} = \frac{1}{2} [3(1-2) + 8(2-1) + 7(1-1)]$$

$$= \frac{1}{2} (3 \times -1 + 8 \times 1 + 7 \times 0)$$
$$= \frac{1}{2} [-3 + 8] = \frac{5}{2} \text{ sq. units.}$$

Area ΔACD

$$\Delta_{ACD} = \frac{1}{2} [3(2-3) + 7(3-1) + 5(1-2)]$$
$$= \frac{1}{2} [3 \times -1 + 7 \times 2 + 5 \times -1]$$
$$= \frac{1}{2} [-3 + 14 - 5]$$
$$= 3 \text{ units}$$

Area
$$\square_{ABCD} = \frac{5}{2} + 3 = \frac{11}{2}$$
 sq. units.

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HOTS QUESTIONS

1. Find the ratio is which the line segment joining the points A(3, -3) and B(-2, 7) is divided by x-axis. Also find the co-ordinates of the point of division. Ans: [CBSE 0.D. 2014]

We have A(3, -3) and B(-2, 7)

At any point on x-axis y-coordinate is always zero. So, let the point be (x, 0) that divides line segment AB in ratio k:1.

Now
$$(x,0) = \left(\frac{-2k+3}{k+1}, \frac{7k-3}{k+1}\right)$$

 $\frac{7k-3}{k+1} = 0$
 $7k-3 = 0 \Rightarrow k = \frac{3}{7}$

The line is divided in the ratio of 3 : 7

Now $\frac{-2k+3}{k+1} = x$ $\frac{-2 \times \frac{3}{7} + 3}{\frac{3}{7} + 1} = x$ $\frac{-6+21}{3+7} = x$ $\frac{15}{10} = x$ $x = \frac{3}{2}$

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The coordinates of the point is $\left(\frac{3}{2},0\right)$.

2. Determine the ratio in which the straight line x-y-2=0 divides the line segment joining (3, -1)and (8,9).

Let co-ordinates of P be (x_1, y_1) and it divides line ABin the ratio k:1.

Now

$$y_1 = \frac{9k - 1}{k + 1}$$

 $x_1 = \frac{8k+3}{k+1}$

Since point $P(x_1, y_1)$ lies on line x - y - 2 = 0, so coordinates of P must satisfy the equation of line.

0

Thus
$$\frac{8k+3}{k+1} - \frac{9k-1}{k+1} - 2 =$$

$$8k + 3 - 9k + 1 - 2k - 2 = 0$$
$$-3k + 2 = 0$$
$$k = \frac{2}{3}$$

So, line x - y - 2 = 0 divides AB in the ratio 2:3

The line segment joining the points A(3,2) and B(5,1)3. is divided at the point P in the ratio 1:2 and P lies on the line 3x - 18y + k = 0. Find the value of k. [Board Term-2, 2012 Set (I)] Ans :

Let co-ordinates of P be (x_1, y_1) and it divides line AB in the ratio 1:2.

$$\begin{array}{c|c} & P \\ A \longleftarrow & + \\ (3,2) & 1:2 \\ \end{array} \xrightarrow{} B \\ (5,1) \end{array}$$

$$x_{1} = \frac{mx_{2} + nx_{1}}{m+n} = \frac{1 \times 5 + 2 \times 3}{1+2} = \frac{11}{3}$$
$$y_{2} = \frac{my_{2} + ny_{1}}{m+n} = \frac{1 \times 2 + 2 \times 2}{1+2} = \frac{5}{3}$$

Since point $P(x_1, y_1)$ lies on line 3x - 18y + k = 0, so co-ordinates of P must satisfy the equation of line.

$$3 \times \frac{11}{3} - 18 \times \frac{5}{3} + k = 0$$

 $k = 19$

If R(x,y) is a point on the line segment joining 4. the points P(a, b) and Q(b, a), then prove that x + y = a + b.

As per question line is shown below.

Let point R(x, y) divides the line joining P and Q in the ratio k:1, then we have

 $x = \frac{kb+a}{k+1}$

Adding,

Ans :

$$z + y = \frac{kb + a + ka + b}{k+1}$$
$$= \frac{k(a+b) + (a+b)}{k+1}$$
$$= \frac{(k+1)(a+b)}{k+1} = a+b$$

x+y = a+bHence Proved

(i) Derive section formula. 5.

3

(ii) In what ratio does (-4, 6) divides the line segment joining the point A(-6, 4) and B(3, -8)

 $y = \frac{ka+b}{k+1}$

(i) Section Formula : Let $A(x_1, y_1)$ and $B(x_2, y_2)$ are two points. Let P(x, y) be a point on line, joining A and B, such that P divides it in the ratio $m_1: m_2$.

Now
$$(x,y) = \left(\frac{m_2 x_1 + m_1 x_2}{m_1 + m_2}, \frac{m_2 y_1 + m_1 y_2}{m_1 + m_2}\right)$$



Proof: Let AB be a line segment joining the points. $A(x_1, y_1), B(x_2, y_2).$

Let P divides AB in the ratio $m_1: m_2$. Let P have coordinates (x, y).

Draw AL, PM, PN, \perp to x-axis

It is clear form figure, that

also,

$$PR = PM - RM = y - y_1.$$

$$PS = ON - OM = x_2 - x$$

 $\frac{AR}{PS} = \frac{PR}{BS} = \frac{AP}{PB}$

$$PS = ON - OM = x_2 - x_2$$
$$BS = BN - SN = y_2 - y_2$$

 $\Delta APR \sim \Delta PBS$

 $\frac{AR}{PS} = \frac{AP}{PB}$

Thus

 $AR = LM = OM - OL = x - x_1$

$$\frac{x - x_1}{x_2 - x} = \frac{m_1}{m_2}$$
$$m_2 x - m_2 x_1 = m_1 x_2 - m_1 x$$
$$x = \frac{m_1 x_2 + m_2 x_1}{m_1 + m_2}$$

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and

Now

 $\frac{y - y_2}{y_2 - y} = \frac{m_1}{m_2}$ $y = \frac{m_1 y_2 + m_2 y_1}{m_1 + m_2}$

Thus co-ordinates of *P* are $\left(\frac{m_2 x_1 + m_1 x_2}{m_1 + m_2}, \frac{m_2 y_1 + m_1 y_2}{m_1 + m_2}\right)$

(ii) Assume that (-4, 6) divides the line segment joining the point A(-6, 4) and B(3, -8) in ratio k:1

Using section formula for x co-ordinate we have

$$-4 = \frac{k(3) - 6}{k+1}$$

-4k-4 = 3k-6 \Rightarrow k = $\frac{2}{7}$

6. If the points A(0,1), B(6,3) and C(x,5) are the vertices of a triangle, find the value of x such that area of $\Delta ABC = 10$

Ans :

[CBSE S.A.2 2016 HODM4OL]

We have A(0,1), B(6,3) and C(x,5)Since area of the triangle ABC is 10, we have

$$\frac{1}{2}[0(3-5)+6(5-1)+x(1-3)] = 10$$
$$\frac{1}{2}[0+24-2x] = 10$$

Here area may be negative also. So we have to consider the negative area also.

For positive area

 $24 - 2x = 20 \Rightarrow x = 2$

For negative area,

$$24 - 2x = -20 \implies x = 22$$

7. The co-ordinates of the points A, B and C are (6,3), (-3,5) and (4, -2) respectively. P(x,y) is any points in the plane. Show that $\frac{ar(\Delta PBC)}{ar(\Delta ABC)} = \left|\frac{x+y-2}{7}\right|$ Ans: [Foreign Set I, 2016]

We have A(6,3), B(-3,5), C(4,-2) and P(x,y)Area of ΔPBC ,

$$\operatorname{ar}(\Delta PBC) = \frac{1}{2} |x(7) + 3(2+y) + 4(y-5)|$$
$$= \frac{1}{2} |7x + 7y - 14|$$

Area of ΔABC ,

$$\operatorname{ar}(\Delta ABC) = \frac{1}{2} |6 \times 7 - 3(-5) + 4(3-5)| = \frac{49}{2}$$

Thus
$$\frac{\operatorname{ar}(\Delta PBC)}{\operatorname{ar}(\Delta ABC)} = \frac{\frac{1}{2}(7x + 7y - 14)}{\frac{49}{2}}$$

= $\frac{7(x + y - 2)}{49} = \left|\frac{x + y - 2}{7}\right|$

8. In the given figure, the vertices of $\triangle ABC$ are A(4,6), B(1,5) and C(7,2). A line-segment DE is drawn to intersect sides AB and AC at D and E respectively such that $\frac{AD}{AB} = \frac{AE}{AC} = \frac{1}{3}$. Calculate the area of



 ΔADE and compare it with area of ΔABC .



Ans :

[O.D. Set I, II, III, 2016]

Area of a triangle having vertices $(x_1, y_1), (x_2, y_2)$ and (x_3, y_3) is given by

$$\Delta = \frac{1}{2} [x_1(y_2 - y_3) + x_2(y_3 - y_1) + x_3(y_1 - y_2)]$$

Thus area of triangle ABC is,

$$\Delta_{ABC} = \frac{1}{2} [4(5-2) + 1(2-6) + 7(6-5)]$$
$$= \frac{1}{2} [12 + (-4) + 7] = \frac{15}{2} \text{ sq units}$$

 $\frac{\Delta_{ADE}}{\Delta_{ABC}} = \left(\frac{AD}{AB}\right)^2 = \left(\frac{1}{3}\right)^2 = \frac{1}{9}$

In
$$\triangle ADE$$
 and $\triangle ABC$, we have

$$\frac{AD}{AB} = \frac{AE}{EC} = \frac{1}{3}$$

and $\angle DAE = \angle BAC$

Hence $\Delta DAE \sim \Delta ABC$

Now

$$\frac{\Delta_{ADE}}{\frac{15}{2}} = \frac{1}{9}$$

Area
$$\Delta_{ADE} = \frac{1.5}{2 \times 9} = \frac{5}{6}$$
 Sq. units

Area Δ_{ADE} : $\Delta_{ABC} = \frac{5}{6}: \frac{15}{2} = 1:9$

9. The three vertices of a parallelogram ABCD are A(3,-4), B(-1,-3) and C(-6,2). Find the coordinates of vertex D and find the area of ABCD.
Ans: [Board Term-2, 2013]

Let 4th vertices of parallelogram be D(x, y). As per question the parallelogram is shown below.



Diagonals of a parallelogram bisect each other. Here E is mid-point of AC and BD. From bisection of AC we have

$$E = \left(\frac{3-6}{2}, \frac{-4+2}{2}\right) = \left(\frac{-3}{2}, 1\right) \tag{1}$$

From bisection of BD we have

$$E = \left(\frac{x-1}{2}, \frac{y-3}{2}\right) \tag{2}$$

From (1) and (2) we have

$$\frac{x-1}{2} = -\frac{3}{2} \Rightarrow x = -3 + 1 \Rightarrow x = -2$$

and
$$\frac{y-3}{2} = -1 \Rightarrow y-3 = -2 \Rightarrow y = 1$$

- Thus fourth vertex D is (-2,1)
- Area of $\Delta \, ABC$

$$\Delta_{ABC} = \frac{1}{2} [x_1(y_2 - y_1) + x_2(y_3 - y_1) + x_2(y_1 - y_2)]$$

= $\frac{1}{2} [3(-3-2) - 1(2+4) - 6(-4+3)]$
= $\frac{1}{2} [-15-6+6]$
= $\frac{1}{2} \times (-15) = -\frac{15}{2} = \frac{15}{2}$ sq. units

Since diagonal divides parallelogram into two equal parts, So Area of parallelogram ABCD

$$\square_{ABCD} = 2 \times \Delta_{ABC}$$

= $2 \times \frac{15}{2} = 15$ sq. units

10. The co-ordinates of vertices of Δ ABC are A(1, -1), B(-4,6) and C(-3, -5). Draw the figure and prove that Δ ABC a scalene triangle. Find its area also.
Ans : [Board Term-2, 2014]

As per question diagram is shown below.



The co-ordinates of the vertices of $\triangle ABC$ are A(1, -1), B(-4, 6) and C(-3, -5) respectively Now $AB = \sqrt{(1+4)^2 + (-1-6)^2}$ $= \sqrt{25+49} = \sqrt{74} = \sqrt{74}$ $BC = \sqrt{(-4+3)^2 + (6+5)^2}$ www.cbse.online

$$= \sqrt{1+121} = \sqrt{122} = \sqrt{122}$$
$$AC = \sqrt{(1+3)^2 - (-1+5)^2}$$
$$= \sqrt{16+16} = 4\sqrt{2}$$

Since $AB \neq BC \neq AC$ triangle ΔABC is scalene. Now, area of ΔABC ,

$$= \frac{1}{2} [1(6+5) + (-4)(-5+1) + (-3)(-1-6)]$$
$$= \frac{1}{2} [11+16+21] = 24$$
 sq. units

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Ans :

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11. (1, -1), (0, 4) and (-5, 3) are vertices of a triangle. Check whether it is a scalene triangle, isosceles triangle or an equilateral triangle. Also, find the length of its median joining the vertex (1, -1) the mid-point of the opposite side.

[Board Term-2, 2015]

Let the vertices of $\triangle ABC$ be A(1, -1), B(0,4) and C(-5,3). Let D(x, y) be mid point of BC. Now the triangle is shown below.



Using distance formula, we get

 $AB = \sqrt{(1-0)^2 + (-1-4)^2} = \sqrt{1+5^2} = \sqrt{26}$ $BC = \sqrt{(-5,0)^2 + (3-4)^2} = \sqrt{25+1} = \sqrt{26}$ $AC = \sqrt{(-5-1)^2 + (3+1)^2} = \sqrt{36+16} = 2\sqrt{13}$ Since $AB = BC \neq AC$, triangle $\triangle ABC$ is isosceles. Now, using mid-section formula, the co-ordinates of mid-point of *BC* are

$$x = \frac{-5+0}{2} = -\frac{5}{2}$$
$$y = \frac{3+4}{2} = \frac{7}{2}$$
$$D(x,y) = \left(-\frac{5}{2}, \frac{7}{2}\right)$$

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Length of median AD

$$AD = \sqrt{\left(\frac{-5}{2} - 1\right)^2 + \left(\frac{7}{2} + 1\right)^2}$$
$$= \sqrt{\left(\frac{-7}{2}\right) + \left(\frac{9}{2}\right)^2}$$
$$= \sqrt{\frac{130}{4}} = \frac{\sqrt{130}}{2} unit^2$$
median *AD* is $\frac{\sqrt{130}}{2}$ units.

Thus length of 2

12. If $a \neq b \neq 0$, prove that the points $(a, a^2), (b, b^2), (0, 0)$ will not be collinear.

Ans :

If three points are collinear, then area covered by given points must be zero.

[Delhi Set I, II, III 2017]

area
$$= \frac{1}{2} [a(b^2 - 0) + b(0 - a^2) + 0(a^2 - b^2)]$$
$$= \frac{1}{2} [ab^2 - a^2b + 0]$$
$$= \frac{1}{2} [ab(b - a)] \neq 0 \text{ as } a \neq b \neq 0$$

Hence, the given points are not collinear.

- **13**. If the points A(k+1,2k), B(3k,2k+3)and C(5k-1,5k) are collinear, then find the value of k. Ans : [Delhi Set I, II, III, 2017]
- **14**. If the points A(k+1,2k), B(3k,2k+2)and C(5k-1,5k) are collinear, then find the value of k. [Outside Delhi, Set-II, 2017] Ans :

If three points are collinear, then area covered by given points must be zero.

Thus area

1

$$\frac{1}{2}[x_1(y_2 - y_3) + x_2(y_3 - y_1) + x_3(y_1 - y_2)] = 0$$

$$x_1(y_2 - y_3) + x_2(y_3 - y_1) + x_2(y_1 - y_2) = 0$$
Here $x_1 = k + 1, x_2 = 3k, x_3 = 5k - 1$

$$y_1 = 2k, y_2 = 2k + 3, y_3 = 5k.$$

$$(k+1)(2k+3-5k) + 3k(5k-2k) + (5k-1)(2k-2k-3) = 0$$

$$(k+1)(3-3k) + 3k(3k) + (5k-1)(-3) = 0$$

$$3(1+k)(1-k) + 3(k)(3k) - 3(5k-1) = 0$$

$$3[1-k^2 + 3k^2 - 5k + 1] = 0$$

$$2k^2 - 5k + 2 = 0$$

$$2k^2 - 4k - k + 2 = 0$$

$$2k(k-2) - 1(k-2) = 0$$

$$(2k-1)(k-2) = 0$$

Thus k = 2 and $\frac{1}{2}$.

15. Thus k = 2 and $\frac{1}{2}$. The points A(4, -2), B(7, 2), C(0, 9)and D(-3,5) from a parallelogram. Find the length of altitude of the parallelogram on the base AB.

[Sample Question Paper 2017] Ans :

Let the height of parallelogram taking AB as based be h.

Now

Ans:

$$AB = \sqrt{(7-4)^2 + (2+2)^2}$$

= $\sqrt{3^2 + 4^2} = \sqrt{9+16}$
= 5 units

 $(4)^2 + (2 + 2)^2$

Area of ΔABC

$$\Delta_{ABC} = \frac{1}{2} [x_1(y_2 - y_1) + x_2(y_3 - y_1) + x_2(y_1 - y_2)]$$

= $\frac{1}{2} [4(2 - 9) + 7(9 + 2) + 0(2 - 2)]$
= $\frac{1}{2} \times 49 = \frac{49}{2}$ sq. units
Now, $\frac{1}{2} \times AB \times h = \frac{49}{2}$
 $\frac{1}{2} \times 5 \times h = 49$
 $h = \frac{49}{5} = 9.8$ units.

16. Point (-1, y) and B(5, 7) lie on a circle with centre O(2, -3y). Find the values of y. Hence find the radius of the circle.

[Delhi CBSE, Term-2, 2014]

Since, A(-1, y) and B(5,7) lie on a circle with centre O(2, -3y), OA and OB are the radius of circle and are equal. Thus

$$OA = OB$$

$$\sqrt{(-1-2)^2 + (y+3y)^2} = \sqrt{(5-2)^2 + (7+3y)^2}$$

$$9 + 16y^2 = 9y^2 + 42y + 58$$

$$y^2 - 6y - 7 = 0$$

$$(y+1)(y-7) = 0$$

$$y = -1,7$$

When y = -1, centre is O(2, -3y) = (2,3) and radius $OB = \left| \sqrt{(5-2)^2 + (7-3)^2} \right|$

$$=\sqrt{9+16} = 5$$
 unit

When y = 7, centre is O(2, -3y) = (2, -21) and radius

$$OB = \left| \sqrt{(2-5)^2 + (-21-7)^2} \right| \\ = \left| \sqrt{9+784} \right| = \sqrt{793} \text{ unit}$$

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